



# Mark Scheme (Results)

## Summer 2026

Pearson Edexcel International GCSE

In Mathematics B (4MB1) Paper 01R

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

- **Types of mark**

- M marks: method marks
- A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)

- **Abbreviations**

- cao – correct answer only
- ft – follow through
- isw – ignore subsequent working
- SC – special case
- oe – or equivalent (and appropriate)
- dep – dependent
- indep – independent
- awrt – answer which rounds to
- eeoo – each error or omission

- **No working**

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

- **With working**

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the “correct” answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review.

If there is a choice of methods shown, then award the lowest mark, unless the subsequent working makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

- **Ignoring subsequent work**

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

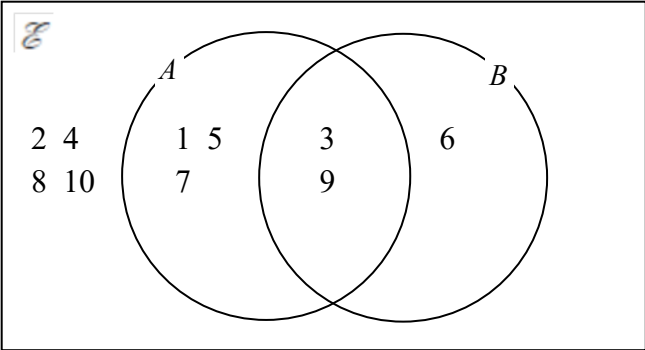
Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

- **Parts of questions**

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

| Question | Working                                                   | Answer | Mark | Notes                                                                                                                                                                                                                                        |
|----------|-----------------------------------------------------------|--------|------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1        | $\frac{18}{45} [= 0.4]$ oe or $\frac{45}{60} [= 0.75]$ oe |        | 2    | M1 Speed in km/min or time in hours found.<br>Allow a calculation to be in km/sec ie $\frac{18}{2700}$<br>Allow for correct fraction or decimal seen. Ignore units written.<br>Look for as part of a calculation eg $\frac{18}{\frac{3}{4}}$ |
|          | cas                                                       | 24     |      | A1 cao                                                                                                                                                                                                                                       |
|          |                                                           |        |      | <b>Total 2 marks</b>                                                                                                                                                                                                                         |

|   |                                                                                                    |                  |   |                                                                                                                                                                                                                                                                                                                                                                                                                               |
|---|----------------------------------------------------------------------------------------------------|------------------|---|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 2 | $1 + 2 [= 3]$ <b>and</b> $\frac{8}{12} + \frac{3}{12}$ oe or<br>$\frac{20}{12} + \frac{27}{12}$ oe |                  | 2 | M1 Adding whole parts <b>and</b> expressing fractional parts with common denominator or<br>expressing as improper fractions with a common denominator.<br>Accept sum with shared denominator or which shows working<br>eg $\frac{2 \times 4 + 1 \times 3}{12}$ eg $\frac{5 \times 4}{3 \times 4} + \frac{9 \times 3}{4 \times 3}$<br>Do not accept eg $\frac{2}{3} \times 4$ $\frac{1}{4} \times 3$ unless clearly recovered. |
|   | wr                                                                                                 | $3\frac{11}{12}$ |   | A1 cao<br>isw eg decimals after a correct answer.                                                                                                                                                                                                                                                                                                                                                                             |
|   |                                                                                                    |                  |   | <b>Total 2 marks</b>                                                                                                                                                                                                                                                                                                                                                                                                          |

|   |                                                                                      |  |   |                                                          |
|---|--------------------------------------------------------------------------------------|--|---|----------------------------------------------------------|
| 3 |  |  | 2 | B2 Fully correct<br>(B1 2 or 3 out of 4 correct regions) |
|   |                                                                                      |  |   | <b>Total 2 marks</b>                                     |

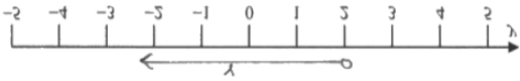
| Question | Working                                                                                                                               | Answer                  | Mark | Notes                                                                                                                                                                                                                                                                |
|----------|---------------------------------------------------------------------------------------------------------------------------------------|-------------------------|------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 4        | $\text{Gradient} = \frac{8[-0]}{[0]-6} \left[ -\frac{8}{6} = -\frac{4}{3} \right] \text{oe}$ or $y = mx + 8$<br>or $-\frac{4}{3}x$ oe |                         | 2    | M1 Correct method to find gradient or correct gradient<br>$y = mx + 8$ seen<br>or $-\frac{4}{3}x$ oe seen                                                                                                                                                            |
|          | cas                                                                                                                                   | $y = -\frac{4}{3}x + 8$ |      | A1 oe in the form $y = mx + c$ (allow $y = -1.3(33\dots)x + 8$ )<br>For a decimal allow 1.3 or better eg $1.\dot{3}$ or 1.33<br>Allow 8 to be $\frac{24}{3}$ oe<br>Allow<br>$-\frac{4}{3}x + 8$ on the answer line, only if $y =$ seen at least once in the working. |
|          |                                                                                                                                       |                         |      | <b>Total 2 marks</b>                                                                                                                                                                                                                                                 |

|   |                                 |                   |   |                                                                                                                                                                                                         |
|---|---------------------------------|-------------------|---|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 5 | $\frac{3 - (-4)}{3^2 + (-4)^2}$ |                   | 2 | M1 Substitute into formula, must have correct signs, accept<br>$\frac{3+4}{3^2+4^2}$ or $\frac{3+4}{9+16}$ or $\frac{7}{n}$ or $\frac{m}{25}$ $m, n$ are integers<br>Missing brackets may be recovered. |
|   | cas                             | $\frac{7}{25}$ oe |   | A1 oe eg 0.28<br>isw after correct answer seen                                                                                                                                                          |
|   |                                 |                   |   | <b>Total 2 marks</b>                                                                                                                                                                                    |

| Question |  | Working                                      | Answer | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |
|----------|--|----------------------------------------------|--------|------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 6        |  | $\frac{1}{2} \times (x+10) \times 5 = 45$ oe |        | 3    | <p>M1 forming correct equation in <math>x</math><br/>           Allow any correct equation where there is already a partial rearrangement.<br/>           Eg <math>\frac{1}{2} \times (x+10) = 9</math>   Eg <math>(x+10) = \frac{45 \times 2}{5}</math><br/>           Condone splitting into a rectangle and 2 triangles or 2 rectangles as follows:<br/> <math>45 = \left[ 2 \times \frac{1}{2} \right] \times 5 \left( \frac{10-x}{2} \right) + 5x</math><br/>           Condone use of eg <math>a</math> or <math>b</math> for <math>x</math></p> |
|          |  | $[x =] \frac{2 \times 45}{5} - 10$ oe        |        |      | <p>M1 dep on previous M1 correct order of operations to isolate <math>x</math><br/>           May imply the previous method mark<br/>           This may be done in stages.</p>                                                                                                                                                                                                                                                                                                                                                                        |
|          |  | cas                                          | 8      |      | A1 cao                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |
|          |  |                                              |        |      | <b>Total 3 marks</b>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |

|   |     |  |                                                |   |                                                |
|---|-----|--|------------------------------------------------|---|------------------------------------------------|
| 7 | (a) |  | $\begin{pmatrix} 4 & 2 \\ 2 & 1 \end{pmatrix}$ | 2 | B2 Fully correct<br>(B1 2 or 3 values correct) |
|   | (b) |  | 3                                              | 1 | B1 cao<br>3 only                               |
|   |     |  |                                                |   | <b>Total 3 marks</b>                           |

|   |     |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |     |    |                                                      |    |   |    |    |   |    |    |  |   |   |    |  |   |   |  |  |   |   |  |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
|---|-----|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|----|------------------------------------------------------|----|---|----|----|---|----|----|--|---|---|----|--|---|---|--|--|---|---|--|---|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 8 | (a) | <div><div><div><div><div>24 = 2<sup>3</sup> × 3</div><div>or 24 = 2<sup>2</sup> × 6</div><div>or 24</div></div><div><div>8</div><div>2</div><div>4</div><div>2</div><div>2</div></div></div><div><div><div>54 = 2 × 3<sup>3</sup></div><div>or 54 = 6 × 3<sup>2</sup></div><div>or 54</div></div><div><div>12</div><div>2</div><div>6</div><div>2</div><div>3</div></div></div><div><div><div>54</div><div>2</div><div>27</div><div>3</div><div>9</div><div>3</div><div>3</div></div><div><div>54</div><div>3</div><div>18</div><div>2</div><div>9</div><div>3</div><div>3</div></div></div></div><div>or</div><div><table><tr><td>2</td><td>24</td><td>54</td><td>or</td><td>3</td><td>24</td><td>54</td></tr><tr><td>3</td><td>12</td><td>27</td><td></td><td>2</td><td>8</td><td>18</td></tr><tr><td></td><td>4</td><td>9</td><td></td><td></td><td>4</td><td>9</td></tr></table></div><div>or complete list of factors of 24 <b>and</b> 54</div><div>or</div><div><div><div><div>2</div><div>2</div></div><div><div>2</div><div>3</div></div><div><div>3</div><div>3</div></div></div></div></div> | 2   | 24 | 54                                                   | or | 3 | 24 | 54 | 3 | 12 | 27 |  | 2 | 8 | 18 |  | 4 | 9 |  |  | 4 | 9 |  | 2 | <div>M1 correct attempt to split either 24 or 54 into prime factors<br/>or prime factor tree (which may stop at last two factors)<br/>eg<div><div>54</div><div>2</div><div>27</div><div>3</div><div>9</div></div></div> <div>or diagram as shown, with prime factorisation as far as 4 and 9</div> <div>or complete list of factors of 24 <b>and</b> 54<br/>(condone 1, 24 and 54 not present)<br/>or correct Venn diagram as shown (can be missing the rectangle).</div> <div>Award for working seen in part (b) if not awarded in (a)</div> |
| 2 | 24  | 54                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | or  | 3  | 24                                                   | 54 |   |    |    |   |    |    |  |   |   |    |  |   |   |  |  |   |   |  |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
| 3 | 12  | 27                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |     | 2  | 8                                                    | 18 |   |    |    |   |    |    |  |   |   |    |  |   |   |  |  |   |   |  |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
|   | 4   | 9                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |     |    | 4                                                    | 9  |   |    |    |   |    |    |  |   |   |    |  |   |   |  |  |   |   |  |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
|   |     | wr                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 6   |    | A1 cao do not accept 2 × 3                           |    |   |    |    |   |    |    |  |   |   |    |  |   |   |  |  |   |   |  |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
|   | (b) |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 216 | 1  | B1 cao do not accept 2 <sup>3</sup> × 3 <sup>3</sup> |    |   |    |    |   |    |    |  |   |   |    |  |   |   |  |  |   |   |  |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
|   |     |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |     |    | Total 3 marks                                        |    |   |    |    |   |    |    |  |   |   |    |  |   |   |  |  |   |   |  |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |

| Question | Working                                                                                                                                                                       | Answer            | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                                                       |
|----------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------|------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 9        | (a)<br>$4x < 13 - 3$ or $4x < 10$ oe<br>eg $2x < 5$ eg $3 - 13 < -4x$<br>or<br>$\frac{3}{4} + \frac{[4]x}{[4]} < \frac{13}{4}$ oe eg $0.75 + x < 3.25$<br>or $\frac{5}{2}$ oe |                   | 2    | M1 correctly isolates term in $x$<br><br>or for correctly dividing through by 4<br><br>or for $\frac{5}{2}$ oe with no inequality or an incorrect inequality or equals symbol                                                                                                                                                                                                                               |
|          | cas                                                                                                                                                                           | $x < \frac{5}{2}$ |      | A1 oe eg $\frac{5}{2} > x$ $x < \frac{10}{4}$<br>Allow a correctly inequality, then incorrectly processed<br>eg $x < \frac{5}{2}$ followed by eg $x < 0.5$ eg $x < 10$ will get A1<br>Allow this to be awarded in the body of working.<br><br>do not isw when there is misunderstanding<br>$x < \frac{5}{2}$ oe followed by $\frac{5}{2}$ oe is A0<br>$x = \frac{5}{2}$ oe is A0 $x > \frac{5}{2}$ oe is A0 |
|          | (b)<br>                                                                                   |                   | 1    | B1 cao<br>Accept anything that has an open circle at 2, with an arrow pointing in the correct direction. Allow “(“ to represent an open circle.<br>Eg<br><br>as arrow indicates this continues beyond where the line stops.                                                                                            |
|          |                                                                                                                                                                               |                   |      | <b>Total 3 marks</b>                                                                                                                                                                                                                                                                                                                                                                                        |

| Question |  | Working | Answer                                    | Mark | Notes                                                                                                           |
|----------|--|---------|-------------------------------------------|------|-----------------------------------------------------------------------------------------------------------------|
| 10       |  |         | $x \geq 4$<br>oe eg<br>$x - 4 \geq 0$     | 3    | B3 All 3 correct<br>B2 Any 2 correct<br>B1 Any 1 correct<br><br>Accept equivalents, condone strict inequalities |
|          |  |         | $y \geq x + 3$<br>oe eg<br>$y - x \geq 3$ |      |                                                                                                                 |
|          |  | cas     | $x + y \leq 4$<br>oe eg<br>$y \leq 4 - x$ |      |                                                                                                                 |
|          |  |         |                                           |      | SC1 – all three inequalities incorrect way round, strict or not                                                 |
|          |  |         |                                           |      | <b>Total 3 marks</b>                                                                                            |

| Question |  | Working                                                                                       | Answer | Mark | Notes                                                                                                                                                                                                                                                               |
|----------|--|-----------------------------------------------------------------------------------------------|--------|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 11       |  | $\frac{80}{360} \times 2 \times \pi \times 5 \left[ = \frac{20}{9} \pi = 6.981... \right]$ oe |        | 3    | M1 Correct method to find arc length<br>Watch for this done in parts.<br>If miscalculation during, <b>award marks for method</b><br>eg<br>$2 \times \pi \times 5 [= 8.281...]$ correct method, incorrect processing]<br>$\frac{4}{9} \times "8.281"$ gets this mark |
|          |  | "6.981..." + $2 \times 5$ [=16.981] oe                                                        |        |      | M1 Add on straight edges to their arc length.<br>It should be clear they're adding the 2 straight edges onto something they think is the arc length (ie nothing to contradict this is the arc length).                                                              |
|          |  | cas                                                                                           | 17     |      | A1 awrt 17<br><br>Watch out for incorrect method of finding the area which also leads to a value of 17 (to 2sf)<br>17.4532.....                                                                                                                                     |
|          |  |                                                                                               |        |      | <b>Total 3 marks</b>                                                                                                                                                                                                                                                |

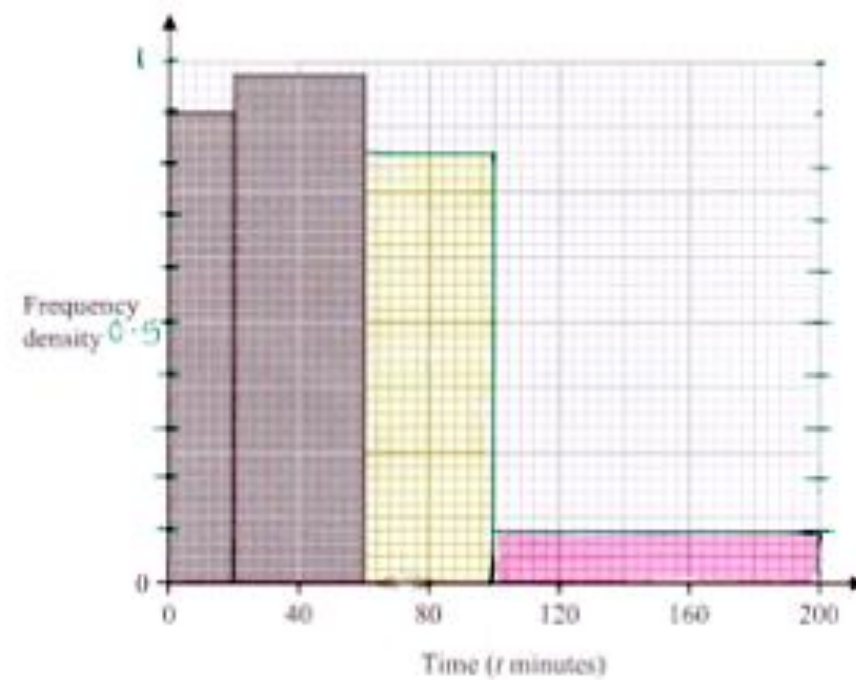
| Question | Working                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | Answer   | Mark | Notes                                                                                                                                                                                  |
|----------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 12       | <p>Frequency density of <math>\frac{18}{20}</math> oe eg 0.9 or <math>\frac{33}{40}</math> oe eg 0.825 seen by the table<br/>or<br/>in working<br/>or<br/>on the graph</p> <p>or<br/>any correct missing frequency or frequency density indicated in table, on graph or in working (39 or 10)</p> <p>or<br/>any correct FD on the vertical axis where the height of 1 small square is <math>0.025 = \frac{1}{40}</math> oe<br/>eg 8 cm to 1 FD</p> <p>or<br/>eg 1 cm<sup>2</sup> to 2.5 frequency</p> |          | 3    | <p>M1 Method to find either a frequency for the table or height of a bar or correct frequency density.</p> <p>Any correct missing frequency or frequency density implies this mark</p> |
|          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 39 or 10 |      | A1 indicated on table, on graph or in working.                                                                                                                                         |
|          | <p>cas<br/>Bar from 60-100 height 0.825 (33 small squares), and<br/>Bar from 100-200 height 0.1 (4 small squares)</p>                                                                                                                                                                                                                                                                                                                                                                                 |          |      | A1                                                                                                                                                                                     |
|          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |          |      | <b>Total 3 marks</b>                                                                                                                                                                   |

| Time ( $t$ minutes) | Number of students |
|---------------------|--------------------|
| $0 \leq t < 20$     | 18                 |
| $20 \leq t < 60$    | 39                 |
| $60 \leq t < 100$   | 33                 |
| $100 \leq t < 200$  | 10                 |

FD

$$\frac{18}{20} = \frac{9}{10} = \frac{36}{40} = 0.9$$

$$\frac{33}{40} = 0.825$$



| Question | Working                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | Answer        | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |
|----------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 13       | $\left[ x = \right] \frac{1+\sqrt{7}}{\frac{1}{2}(6-2\sqrt{7})} \left[ = \frac{1+\sqrt{7}}{3-\sqrt{7}} = \frac{2+2\sqrt{7}}{6-2\sqrt{7}} \right] \text{ or } \left[ \frac{1}{2}x = \right] \frac{1+\sqrt{7}}{(6-2\sqrt{7})} \text{ oe}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |               | 3    | <p>M1<br/>Any correct expression shown oe<br/>For this question, completely ignore labelling of x or <math>\frac{1}{2}x</math></p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |
|          | <p>Finding x <math>\frac{1+\sqrt{7}}{3-\sqrt{7}} \times \frac{3+\sqrt{7}}{3+\sqrt{7}} = \frac{3+3\sqrt{7}+\sqrt{7}+7}{9[+3\sqrt{7}-3\sqrt{7}]-7} \text{ or } \frac{10+4\sqrt{7}}{2}</math></p> <p><math>\frac{1+\sqrt{7}}{3-\sqrt{7}} \times \frac{-3-\sqrt{7}}{-3-\sqrt{7}} = \frac{-3-3\sqrt{7}-\sqrt{7}-7}{-9[+3\sqrt{7}-3\sqrt{7}]+7}</math></p> <p>oe eg <math>\frac{-10-4\sqrt{7}}{-2} \text{ or } \frac{10+4\sqrt{7}}{2}</math></p> <p>oe eg <math>\frac{2+2\sqrt{7}}{6-2\sqrt{7}} \times \frac{6+2\sqrt{7}}{6+2\sqrt{7}} = \frac{12+12\sqrt{7}+4\sqrt{7}+4 \times 7}{36[+12\sqrt{7}-12\sqrt{7}]-28} \text{ or } \frac{40+16\sqrt{7}}{8}</math></p> <p>or Finding <math>\frac{1}{2}x</math></p> <p><math>\frac{1+\sqrt{7}}{6-2\sqrt{7}} \times \frac{6+2\sqrt{7}}{6+2\sqrt{7}} = \frac{6+6\sqrt{7}+2\sqrt{7}+14}{36[+12\sqrt{7}-12\sqrt{7}]-28} \text{ or } \frac{20+8\sqrt{7}}{8}</math></p> <p>oe eg <math>\frac{1+\sqrt{7}}{6+2\sqrt{7}} \times \frac{-6-2\sqrt{7}}{-6-2\sqrt{7}} = \frac{-6-6\sqrt{7}-2\sqrt{7}-14}{-36[+12\sqrt{7}-12\sqrt{7}]-28}</math></p> <p>or <math>\frac{-20-8\sqrt{7}}{-8} \text{ or } \frac{20+8\sqrt{7}}{8}</math></p> |               |      | <p>M1 For rationalising any of <math>\frac{1+\sqrt{7}}{\frac{1}{2}(6-2\sqrt{7})} \frac{1+\sqrt{7}}{3-\sqrt{7}} \frac{2+2\sqrt{7}}{6-2\sqrt{7}} \text{ oe}</math></p> <p>or <math>\frac{1+\sqrt{7}}{(6-2\sqrt{7})} \text{ oe}</math></p> <p>a <b>correct</b> product stated to rationalise the denominator<br/><b>and</b> processing with at least 2 out of 4 numerator terms correct and correct processing of denom allow any mix of processing – full evaluation doesn't need to be seen eg accept <math>4 \times 7</math> for <math>28 (\sqrt{7})^2</math> for 7</p> <p>eg <math>\frac{10+3\sqrt{7}+\sqrt{7}}{9-7}</math></p> <p>eg <math>\frac{10-7\sqrt{7}+\sqrt{7}}{9-(\sqrt{7})^2}</math></p> <p>would imply 2 out of 4 terms correct.</p> |
|          | wr                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | $5+2\sqrt{7}$ |      | <p>A1<br/>accept<br/><math>a=5, b=2, c=7</math></p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
|          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |               |      | <b>Total 3 marks</b>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |

| Question |     | Working                                                                                              | Answer | Mark | Notes                                                                                                                                                                                        |
|----------|-----|------------------------------------------------------------------------------------------------------|--------|------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 14       | (a) | $\frac{1926}{1.2}$ or $\frac{1926}{120} \times 100$ oe eg $\frac{1926}{6} \times 5$<br>$1.2x = 1926$ |        | 2    | M1 Complete method to reverse percentage increase<br>or a correct equation in $x$<br>Condone eg $\frac{1926}{120\%}$ eg $\frac{1926}{(1 + 20\%)}$<br>Do not condone this, without the % sign |
|          |     | cas                                                                                                  | 1605   |      | A1 cao                                                                                                                                                                                       |
|          | (b) | $\frac{1926}{1.07}$ oe                                                                               |        | 2    | M1 Correct method to change \$1926 into euros                                                                                                                                                |
|          |     | cas                                                                                                  | 1800   |      | A1 cao                                                                                                                                                                                       |
|          |     |                                                                                                      |        |      | <b>Total 4 marks</b>                                                                                                                                                                         |

|    |     |                                                                                                                      |                        |   |                                                                                      |
|----|-----|----------------------------------------------------------------------------------------------------------------------|------------------------|---|--------------------------------------------------------------------------------------|
| 15 | (a) | $10.8 \times 10^{201}$ or $1.08 \times 10^n$ or $k \times 10^{202}$                                                  |                        | 2 | M1 $n$ must be an integer and $1, k < 10$                                            |
|    |     | cas                                                                                                                  | $1.08 \times 10^{202}$ |   | A1 cao                                                                               |
|    | (b) | $0.9 \times 10^{101}$ or $12 \times 10^{100}$ or $21 \times 10^{100}$ or<br>$2.1 \times 10^m$ or $q \times 10^{101}$ |                        |   | M1 Express both numbers with same exponent where $m$ is an integer and $1, q < 10$ . |
|    |     | cas                                                                                                                  | $2.1 \times 10^{101}$  | 2 | A1 cao                                                                               |
|    |     |                                                                                                                      |                        |   | <b>Total 4 marks</b>                                                                 |

| Question |     | Working                                                                                                                                                                                                                                                                                                                                                                                                            | Answer                                                                                                                                               | Mark | Notes                                                                                                                                   |
|----------|-----|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------|------|-----------------------------------------------------------------------------------------------------------------------------------------|
| 16       | (a) |                                                                                                                                                                                                                                                                                                                                                                                                                    | $\pi \times 6^2 \times 12 [= 432\pi]$ or<br>$\pi \times \left(\frac{12}{2}\right)^2 \times 12 [= 432\pi]$<br>or $\pi \times 36 \times 12 [= 432\pi]$ | 1    | B1 one of the correct expressions only                                                                                                  |
|          | (b) | $\pi r^2 \times 2r = (432 - 416)\pi [= 16\pi]$ oe<br>or<br>$\pi \left(\frac{d}{2}\right)^2 \times d = (432 - 416)\pi [= 16\pi]$ oe<br>or<br>$\left[ (432 - 416)\pi = \pi r^2 h \Rightarrow h = \frac{16}{r^2} \right]$<br>$\left[ \frac{h}{12} = \frac{r}{6} \right] \Rightarrow \frac{r^2}{12} = \frac{r}{6}$ oe eg $\frac{16\pi}{12} = \frac{r}{6}$<br>where $r$ and $h$ are radius and height of small cylinder |                                                                                                                                                      | 3    | M1 correct equation involving $r$ or $d$ only<br>( $r$ is radius $d$ is diameter of small cylinder)<br>Allow any letters for $r$ or $d$ |
|          |     | $[r =] 2$                                                                                                                                                                                                                                                                                                                                                                                                          |                                                                                                                                                      |      | M1 Dep on 1 <sup>st</sup> M<br>solves for $r$ or $d$ (allow 1 processing error)                                                         |
|          |     | cas                                                                                                                                                                                                                                                                                                                                                                                                                | 4                                                                                                                                                    |      | A1                                                                                                                                      |

|      |     |                                                                                                                                                                                                                                                                                                                                                                                                                                              |   |  |                                                                                                                                                                                                                                                       |
|------|-----|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---|--|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ALT1 | (b) | $\frac{(432-416)\pi}{432\pi} \left[ = \frac{16\pi}{432\pi} = \frac{1}{27} \right] \text{ oe}$ <p><b>and</b> <math display="block">\sqrt[3]{\frac{(432-416)\pi}{432\pi}} \left[ = \frac{1}{3} \right] \text{ oe}</math> or <math display="block">\frac{432\pi}{(432-416)\pi} \left[ = \frac{432\pi}{16\pi} = 27 \right] \text{ oe}</math> <b>and</b> <math display="block">\sqrt[3]{\frac{432\pi}{(432-416)\pi}} [= 3] \text{ oe}</math> </p> |   |  | <p>find ratio of volumes of smaller cylinder to original<br/> <b>and</b> find a linear ratio<br/> For <math>16\pi</math> allow awrt 50.3<br/> For <math>416\pi</math> allow awrt 1310<br/> For <math>432\pi</math> allow awrt 1360</p>                |
|      |     | $12 \times \frac{1}{3}''$ or $6 \times \frac{1}{3}''$ oe                                                                                                                                                                                                                                                                                                                                                                                     |   |  | <p>M1 Dep on 1<sup>st</sup> M<br/> use linear ratio to find diameter or radius</p>                                                                                                                                                                    |
|      |     | cas                                                                                                                                                                                                                                                                                                                                                                                                                                          | 4 |  | A1 awrt 4                                                                                                                                                                                                                                             |
| ALT2 | (b) | $\frac{(432-416)\pi}{432\pi} = \left( \frac{d}{12} \right)^3 \text{ oe}$                                                                                                                                                                                                                                                                                                                                                                     |   |  | <p>M1 correct equation involving <math>d</math> only<br/> (<math>d</math> is diameter of small cylinder)<br/> For <math>16\pi, 416\pi, 432\pi</math> allow values as per ALT1<br/> Allow any letter for <math>d</math> (including <math>r</math>)</p> |
|      |     | [d =] 4                                                                                                                                                                                                                                                                                                                                                                                                                                      |   |  | <p>M1 Dep on 1<sup>st</sup> M<br/> solves for <math>d</math> (allow 1 processing error)</p>                                                                                                                                                           |
|      |     | cas                                                                                                                                                                                                                                                                                                                                                                                                                                          | 4 |  | A1 awrt 4                                                                                                                                                                                                                                             |
|      |     |                                                                                                                                                                                                                                                                                                                                                                                                                                              |   |  | <b>Total 4 marks</b>                                                                                                                                                                                                                                  |

| Question |     | Working                                                                                                                      | Answer     | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                                                                |
|----------|-----|------------------------------------------------------------------------------------------------------------------------------|------------|------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 17       | (a) | Examples for B1:<br><br>$2^3 x^6 y^9$<br>$x^5 \times 2^3 \times y^9$<br>$x^6 \times y^9 \times 2^3$<br>$4.5x^6 y^9$          | $8x^6 y^9$ | 2    | B2 For the correct term. Allow in any order eg $x^6 8y^9$<br>8 must not be $2^3$<br>(B1 any 2 terms correct as part of a product of the form $bx^n y^m$ $b, m, n \neq 0$ . Allow 8 to be $2^3$<br>Condone terms with or without of multiplication signs for B1 only eg $x^6 \times y^9 2^3$<br>Only allow transcription errors of the powers or the constant onto the answer line)<br>Do not isw (B1 only)           |
|          | (b) | Examples for B1:<br><br>$3^2 p^8 q^4$<br>$p^8 \times 3^2 \times q^{-2}$<br>$p^6 \times q^4 \times 3^2$<br>$p^8 q^4 \times 6$ | $9p^8 q^4$ | 2    | B2 Allow in any order eg $p^8 q^4 9$<br>Condone $a = 9, m = 8, n = 4$<br>9 must not be $3^2$<br>B1 any 2 terms correct as part of a product of the form $ap^n q^m$ $a, n, m \neq 0$ . Allow 9 to be $3^2$<br>Condone terms with or without of multiplication signs for B1 only eg $p^6 \times q^4 3^2$<br>Only allow transcription errors of the powers or the constant onto the answer line<br>Do not isw (B1 only) |
|          |     |                                                                                                                              |            |      | <b>Total 4 marks</b>                                                                                                                                                                                                                                                                                                                                                                                                 |

| Question | Working                                                                                                                                          | Answer | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |
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| 18       | $\frac{x}{x+1} = \sin 20 [= 0.342]$ oe eg $x = (x+1)\sin 20$<br>eg $\frac{x}{\sin 20} = \frac{x+1}{\sin 90}$                                     |        | 4    | M1 Form correct equation in $x$ using $\sin 20$<br>Allow also $BC$ or a mix of $BC$ and $x$<br><b>Allow <math>\sin 20</math> to be awrt 0.34 throughout.</b><br><br>Allow a processing error for $\sin 20$ if clearly seen written first (general marking principle, if not precluded by the MS)<br>A common error seen will be where a candidate's calculator is in radians and they evaluate $\sin 20$ as 0.912945.....<br>Must be using a number with minimum 2dp.<br>Allow a misevaluation of $\sin 20$ , if $\sin 20$ is seen, throughout, with continued correct working. |
|          | $x = x \sin 20 + \sin 20$<br>oe eg $x - \sin 20 = x \sin 20$<br>eg $0.34(2...)x + 0.34(2...) = x$                                                |        |      | Dep on 1 <sup>st</sup> M1<br>Correctly removes fraction from equation and expands bracket<br>Can imply the previous method mark.                                                                                                                                                                                                                                                                                                                                                                                                                                                |
|          | $x(1 - \sin 20) = \sin 20$<br>oe eg $x(1 - \sin 20) - \sin 20 = 0$<br>eg $[x =] \frac{\sin 20}{1 - \sin 20} = \frac{0.34(2...)}{1 - 0.34(2...)}$ |        |      | Dep on 2 <sup>nd</sup> M1<br>Correctly separates terms in $x$ (or collects if using awrt 0.34)<br>Can imply previous 2 method marks.                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|          | cas                                                                                                                                              | 0.52   |      | A1 awrt 0.52                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |

|      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |      |   |                                                                                                                                                                                                                                                                                                                                                                                                                         |
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| ALT1 | $\left[ (AB) = \sqrt{(x+1)^2 - x^2} = \sqrt{2x+1} \right]$ $\cos 20 = \frac{\sqrt{2x+1}}{x+1} \text{ oe eg } (\cos 20)^2 = \left( \frac{\sqrt{2x+1}}{x+1} \right)^2 \text{ oe}$ <p>or</p> $\frac{\sqrt{2x+1}}{\sin 70} = \frac{x}{\sin 20} \text{ oe eg } \frac{2x+1}{(\sin 70)^2} = \frac{x^2}{(\sin 20)^2} \text{ eg } \frac{\sqrt{2x+1}}{\sin 70} = \frac{x+1}{[\sin 90]}$ <p>or</p> $\tan 20 = \frac{x}{\sqrt{2x+1}} \text{ oe eg } (\tan 20)^2 = \left( \frac{x}{\sqrt{2x+1}} \right)^2 \text{ oe}$ |      | 4 | <p>M1 For a correct equation in <math>x</math> and <math>\sin 20</math> or <math>\cos 20</math> or <math>\tan 20</math></p> <p><math>\sin 20 = 0.34202\dots</math><br/> <math>\cos 20 = 0.93969\dots</math><br/> <math>\tan 20 = 0.36397\dots</math></p> <p><math>(\sin 20)^2 = 0.11697\dots</math><br/> <math>(\cos 20)^2 = 0.88302\dots</math><br/> <math>(\tan 20)^2 = 0.13247\dots</math></p> <p>Allow awrt 2dp</p> |
|      | <p><math>(\cos 20)^2 x^2 + (2(\cos 20)^2 - 2)x + (\cos 20)^2 - 1 [= 0] \text{ oe}</math></p> <p>or</p> <p><math>(\sin 70)^2 x^2 - 2(\sin 20)^2 x - (\sin 20)^2 [= 0] \text{ oe}</math></p> <p>or</p> <p><math>(0.88302\dots)x^2 - (0.23395\dots)x - 0.11697\dots [= 0] \text{ oe}</math></p> <p>or</p> <p><math>x^2 - 2(\tan 20)^2 - (\tan 20)^2 [= 0] \text{ oe}</math></p> <p>or</p> <p><math>x^2 - (0.26494\dots)x - 0.13247\dots [= 0] \text{ oe}</math></p>                                         |      |   | <p>M1 dep on 1<sup>st</sup> M1<br/> For correct 3 term quadratic in <math>\cos 20</math> or <math>\tan 20</math></p> <p>Award if 2 out of 3 terms are correct</p> <p>Don't need to see <math>= 0</math></p> <p>May imply previous M mark with 2 coefficients correct</p> <p>Allow evaluated coefficients awrt<br/> 0.88, 0.23, 0.12, 0.26, 0.13</p>                                                                     |
|      | <p>eg <math>[x =] \frac{-\left(2(\cos 20)^2 - 2\right) \pm \sqrt{\left(\left(2(\cos 20)^2 - 2\right)\right)^2 - 4(\cos 20)^2((\cos 20)^2 - 1)}}{2(\cos 20)^2}</math></p>                                                                                                                                                                                                                                                                                                                                 |      |   | <p>M1 dep on 2<sup>nd</sup> M1 (ie using a 3TQ with 2 out of 3 terms correct)</p> <p>Correct substitution into the quadratic formula</p>                                                                                                                                                                                                                                                                                |
|      | cas                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | 0.52 |   | A1 awrt 0.52                                                                                                                                                                                                                                                                                                                                                                                                            |

|      |                                                                                                                                                                                                                                                                                                      |      |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |
|------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|---|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ALT2 | $\left[ (AB) = \sqrt{(x+1)^2 - x^2} = \sqrt{2x+1} \right]$ $x^2 = (x+1)^2 + (\sqrt{2x+1})^2 - 2(x+1)(\sqrt{2x+1})\cos 20 \text{ oe}$ $\text{oe eg } \cos 20 = \frac{(x+1)^2 + 2x+1 - x^2}{2(x+1)\sqrt{2x+1}}$ <p>or</p> $(\sqrt{2x+1})^2 = (x+1)^2 + x^2 - 2x(x+1)\cos 70$                           |      | 4 | <p>M1 correct equation in <math>x</math> using cosine rule</p> <p><math>\cos 70 = 0.34202\dots</math><br/> <math>\cos 20 = 0.93969\dots</math></p> <p>Allow awrt 2dp</p>                                                                                                                                                                                                                                                                                           |
|      | $2(\cos 20)^2 x^3 + (5(\cos 20)^2 - 4)x^2 + 4((\cos 20)^2 - 4)x + (\cos 20)^2 - 1 [= 0]$ <p>or</p> $(1.76604\dots)x^3 + (0.41511\dots)x^2 - (0.46791\dots)x - 0.11697\dots [= 0] \text{ oe}$ <p>or</p> $(2 - 2\cos 70)x^2 - (2\cos 70)x [= 0]$ <p>or</p> $(1.31595\dots)x^2 - (0.68404\dots)x [= 0]$ |      |   | <p>M1 dep on 1<sup>st</sup> M1<br/> For correct 4 term cubic in <math>\cos 20</math> or quadratic in <math>\cos 70</math></p> <p>Award if 2 out of 4 terms are correct for the cubic or 2 out of 3 terms correct for the quadratic.</p> <p>Don't need to see <math>= 0</math><br/> May imply previous M mark with 2 coefficients correct<br/> Allow evaluated coefficients awrt<br/> 1.77, 0.42, - 0.47, - 0.12, 1.32, 0.68 in the relevant cubic or quadratic</p> |
|      | <p>eg <math>x((2 - 2\cos 70)x - 2\cos 70) [= 0] \text{ oe}</math></p> <p>oe eg <math>[x =] \frac{2\cos 70}{2 - 2\cos 70} \text{ oe}</math></p>                                                                                                                                                       |      |   | <p>M1 for correct factorisation or use of correct substitution into the quadratic formula to solve the 2TQ (with at least one term correct)</p> <p>May be implied by awrt 0.52</p>                                                                                                                                                                                                                                                                                 |
|      | cas                                                                                                                                                                                                                                                                                                  | 0.52 |   | A1 awrt 0.52                                                                                                                                                                                                                                                                                                                                                                                                                                                       |

| Question | Working                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | Answer                           | Mark | Notes                                                                                                                                                                                                             |
|----------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------|------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 19       | $3x^2 + 9x = 3x(x+3)$<br>or<br>$2x^2 + 9x + 9 = (2x+3)(x+3)$                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                  | 4    | M1 Correctly factorises $3x^2 + 9x$<br>or<br>factorises $2x^2 + 9x + 9$ correctly<br><br>May be awarded for factorising after the fractions are added,<br>in which case expect to see $3x(x+3)(x-2)$ in the denom |
|          | $\frac{2x^2 + 9x + 9}{3x^2 + 9x} = \frac{2x+3}{3x}$<br>or<br>$\frac{(2x^2 + 9x + 9)(x-2)}{(3x^2 + 9x)(x-2)} = \frac{2x+3}{3x}$                                                                                                                                                                                                                                                                                                                                                                  |                                  |      | M1<br><br>Correct simplification of the second fraction.<br>May be awarded for simplification after the fractions are added                                                                                       |
|          | $\frac{3x(x-5) + (x-2)(2x+3)}{3x(x-2)}$ oe eg $\frac{3x^2 - 15x}{3x^2 - 6x} + \frac{2x^2 - x - 6}{3x^2 - 6x}$<br>or<br>eg $\frac{(3x^2 + 9x)(x-5)}{(3x^2 + 9x)(x-2)} + \frac{(x-2)(2x^2 + 9x + 9)}{(3x^2 + 9x)(x-2)}$<br>or<br>eg $\frac{3x(x+3)(x-5) + (x-2)(2x+3)(x+3)}{3x(x+3)(x-2)}$<br>or eg $\frac{5x^3 - x^2 - 54x - 18}{3x^3 + 3x^2 - 18x}$<br>or eg $\frac{3x^3 - 15x^2 + 9x^2 - 45x}{3x^3 + 9x^2 - 6x^2 - 18x} + \frac{2x^3 + 9x^2 + 9x - 4x^2 - 18x - 18}{3x^3 + 9x^2 - 6x^2 - 18x}$ |                                  |      | M1 For the correct addition of the 2 correct fractions.<br><br>Must reach a common denominator.<br>This may be as separate fractions.<br><br>Missing brackets must be recovered.<br>May be implied by A1          |
|          | cas                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | $\frac{5x^2 - 16x - 6}{3x(x-2)}$ |      | A1 oe must be simplified<br>eg $\frac{5x^2 - 16x - 6}{3x^2 - 6x}$                                                                                                                                                 |
|          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                                  |      | <b>Total 4 marks</b>                                                                                                                                                                                              |

| Question |     | Working                                                          | Answer         | Mark | Notes                                                                                                                                                                                                                                                                                                                             |
|----------|-----|------------------------------------------------------------------|----------------|------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 20       | (a) | $[f(-2) =]$ eg<br>$(-2)^3 + 7 \times (-2)^2 + 17 \times -2 + 14$ |                | 2    | M1<br><b>If a full substitution is not seen, the minimum we will accept is</b><br>$-8 + 28 - 34 + 14$<br><br>Condone<br>$-2^3 + 7 \times -2^2 + 17 \times -2 + 14 = 0$<br><b>or</b><br>$-2^3 + 7 \times (-2)^2 + 17 \times -2 + 14 = 0$<br>Must see = 0 for either of these<br>Ignore any reference to long division for part (a) |
|          |     | wr                                                               | = 0            |      | A1                                                                                                                                                                                                                                                                                                                                |
|          | (b) | $x^2 + Ax + 7$ or $x^2 + 5x + B$ $A, B > 0$                      |                | 2    | M1 Any 2 terms of the quadratic factor obtained –<br><b>this may be seen awarded for the correct quadratic factor seen in part (a)</b>                                                                                                                                                                                            |
|          |     | cas                                                              | $x^2 + 5x + 7$ |      | A1<br>Do not isw eg if they go on to solve, after seeing the correct quadratic, award A0<br><b>This must be seen in part (b) to be awarded</b>                                                                                                                                                                                    |
|          |     |                                                                  |                |      | <i>Total 4 marks</i>                                                                                                                                                                                                                                                                                                              |

| Question      | Working                                                                                                                                                                                                                                              | Answer                                                                                                              | Mark | Notes                                                                                                                                                                                                                                                                                                                          |
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| 21            | $[\mathbf{NM}] = \begin{pmatrix} 15 & 19 \\ 19 & 24 \end{pmatrix}$                                                                                                                                                                                   |                                                                                                                     | 4    | M1 Attempt to find <b>NM</b> (at least 2 values in the matrix correct)                                                                                                                                                                                                                                                         |
|               | $\left[ \begin{pmatrix} 15 & 19 \\ 19 & 24 \end{pmatrix} \right] = 15 \times 24 - 19 \times 19 [= -1]$<br>For reference<br>$\left[ \mathbf{MN} = \begin{pmatrix} 7 & -9 \\ -25 & 32 \end{pmatrix} \right]$<br>$7 \times 32 - (-9 \times -25) [= -1]$ |                                                                                                                     |      | M1 Correct <b>method</b> to find determinant of their <b>NM</b> (allow their <b>MN</b> )<br>Eg for <b>MN</b><br>$\left[ \begin{pmatrix} 7 & -9 \\ -25 & 32 \end{pmatrix} \right] = 7 \times 32 - (-9) \times (-25) [= -1]$<br>For an incorrect <b>NM</b> or <b>MN</b> , correct working must be shown for their matrix product |
|               | $\left[ (\mathbf{NM})^{-1} = \frac{1}{-1} \right] \begin{pmatrix} 24 & -19 \\ -19 & 15 \end{pmatrix}$                                                                                                                                                |                                                                                                                     |      | M1 ft their <b>NM</b> (allow their <b>MN</b> )<br>This mark is for (ignore the determinant)<br>$\begin{pmatrix} a & b \\ c & d \end{pmatrix} \rightarrow \begin{pmatrix} d & -b \\ -c & a \end{pmatrix}$ with their <b>NM</b> or their <b>MN</b>                                                                               |
|               | cas                                                                                                                                                                                                                                                  | $\begin{pmatrix} -24 & 19 \\ 19 & -15 \end{pmatrix}$<br>or<br>$-\begin{pmatrix} 24 & -19 \\ -19 & 15 \end{pmatrix}$ |      | A1<br><br>Allow<br>eg $-\frac{1}{1} \begin{pmatrix} 24 & -19 \\ -19 & 15 \end{pmatrix}$ or eg $\frac{1}{-1} \begin{pmatrix} 24 & -19 \\ -19 & 15 \end{pmatrix}$                                                                                                                                                                |
| Total 4 marks |                                                                                                                                                                                                                                                      |                                                                                                                     |      |                                                                                                                                                                                                                                                                                                                                |

|                          |  |                                                                                                                                                                                                                                                                                                 |                                                                                                                                                    |   |                                                                                                                                                                                               |
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| <b>21</b><br><b>Alt1</b> |  | $\left[ \left( \begin{array}{cc} 1 & 1 \\ -3 & -4 \end{array} \right) \right] = 1 \times (-4) - 1 \times (-3) [= -1]$ <p>or</p> $\left[ \left( \begin{array}{cc} 3 & -4 \\ 4 & -5 \end{array} \right) \right] = 3 \times (-5) - 4 \times (-4) [= 1]$                                            |                                                                                                                                                    | 4 | M1 correct method to find determinant of <b>M</b> or <b>N</b>                                                                                                                                 |
|                          |  | $\left( \begin{array}{cc} 1 & 1 \\ -3 & -4 \end{array} \right) \rightarrow \left( \begin{array}{cc} -4 & -1 \\ 3 & 1 \end{array} \right) \text{ or }$ $\left( \begin{array}{cc} 3 & -4 \\ 4 & -5 \end{array} \right) \rightarrow \left( \begin{array}{cc} -5 & 4 \\ -4 & 3 \end{array} \right)$ |                                                                                                                                                    |   | M1 correct method to find inverse (ignore determinant) of <b>M</b> or <b>N</b>                                                                                                                |
|                          |  | $\left( \begin{array}{cc} -24 & 19 \\ 19 & -15 \end{array} \right)$                                                                                                                                                                                                                             |                                                                                                                                                    |   | M1 Find $\mathbf{M}^{-1}\mathbf{N}^{-1}$<br>Awarded if at least 2 out of 4 numbers in the final matrix are correct.                                                                           |
|                          |  | cas                                                                                                                                                                                                                                                                                             | $\left( \begin{array}{cc} -24 & 19 \\ 19 & -15 \end{array} \right)$ <p>or</p> $-\left( \begin{array}{cc} 24 & -19 \\ -19 & 15 \end{array} \right)$ |   | A1<br><br>Allow<br>eg $-\frac{1}{1} \left( \begin{array}{cc} 24 & -19 \\ -19 & 15 \end{array} \right)$ or eg $\frac{1}{-1} \left( \begin{array}{cc} 24 & -19 \\ -19 & 15 \end{array} \right)$ |

|            |  |                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                      |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |
|------------|--|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------|---|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 21<br>Alt2 |  | $[\mathbf{NM}] = \begin{pmatrix} 15 & 19 \\ 19 & 24 \end{pmatrix}$                                                                                                                                                                                                                                                                                                            |                                                                                                                      | 4 | M1 Attempt to find <b>NM</b><br>(at least 2 numbers in the matrix correct)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |
|            |  | $\begin{pmatrix} 15 & 19 \\ 19 & 24 \end{pmatrix} \begin{pmatrix} x_1 & x_2 & x_3 \dots \\ y_1 & y_2 & y_3 \dots \end{pmatrix}$ $= \begin{pmatrix} x_1' & x_2' & x_3' \dots \\ y_1' & y_2' & y_3' \dots \end{pmatrix}$                                                                                                                                                        |                                                                                                                      |   | <p>M1 Correct attempt to multiply any 2 by 2 matrix representing their <b>NM</b> by a 2 by <math>n</math> matrix with entries that form coordinates that could make any shape with <math>n</math> sides.</p> <p><b>Entries in the resulting matrix will need to be checked.</b><br/> <b>Allow for 2 correct columns using their NM and their set of coordinates.</b></p> <p>Note it is also possible to just work with a 2 by 2 rather than 2 by <math>n</math> matrix and transform 2 points.</p>                                                                                      |
|            |  | $\begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} x_1' & x_2' & x_3' \dots \\ y_1' & y_2' & y_3' \dots \end{pmatrix}$ $= \begin{pmatrix} x_1 & x_2 & x_3 \dots \\ y_1 & y_2 & y_3 \dots \end{pmatrix} \Rightarrow$ $ax_1' + by_1' = x_1$ $ax_2' + by_2' = x_2$ $ax_3' + by_3' = x_3$ <p>and</p> $cx_1' + dy_1' = y_1$ $cx_2' + dy_2' = y_2$ $cx_3' + dy_3' = y_3$ |                                                                                                                      |   | <p>M1 for <math>\begin{pmatrix} a &amp; b \\ c &amp; d \end{pmatrix} \begin{pmatrix} x_1' &amp; x_2' &amp; x_3' \dots \\ y_1' &amp; y_2' &amp; y_3' \dots \end{pmatrix} = \begin{pmatrix} x_1 &amp; x_2 &amp; x_3 \dots \\ y_1 &amp; y_2 &amp; y_3 \dots \end{pmatrix}</math></p> <p><b>and</b> correctly forming 2 pairs of simultaneous equations.</p> <p>These equations must be correct for their <b>NM</b> and their image and original coordinates.</p> <p>Note it is also possible to just work with a 2 by 2 rather than 2 by <math>n</math> matrix and transform 2 points.</p> |
|            |  |                                                                                                                                                                                                                                                                                                                                                                               | $\begin{pmatrix} -24 & 19 \\ 19 & -15 \end{pmatrix}$ <p>or</p> $-\begin{pmatrix} 24 & -19 \\ -19 & 15 \end{pmatrix}$ |   | <p>A1</p> <p>Allow</p> <p>eg <math>-\frac{1}{1} \begin{pmatrix} 24 &amp; -19 \\ -19 &amp; 15 \end{pmatrix}</math> or eg <math>\frac{1}{-1} \begin{pmatrix} 24 &amp; -19 \\ -19 &amp; 15 \end{pmatrix}</math></p>                                                                                                                                                                                                                                                                                                                                                                        |

| Question |     | Working                                                                                                                                                                                                                                              | Answer             | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                              |
|----------|-----|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------|------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 22       | (a) | $0.3 + 0.1 + 2x + x = 1$ or $\frac{1 - 0.3 - 0.1}{3}$                                                                                                                                                                                                |                    | 2    | M1 Correct equivalent equation<br>or<br>Correct equivalent full method (look for this to be in parts and carry through any processing errors,<br>e.g $0.3 + 0.1 [= 0.31]$ incorrect processing, correct method]<br>$1 - 0.31 [= 0.79]$ correct method again, with now 2 processing errors]<br>$\frac{0.79}{3}$ will be awarded this mark if all of the method is explicitly shown. |
|          |     | cas                                                                                                                                                                                                                                                  | 0.2                |      | A1                                                                                                                                                                                                                                                                                                                                                                                 |
|          | (b) | $0.3 \times 340$ oe                                                                                                                                                                                                                                  |                    | 2    | M1 award for $0.1 \times 340$ or $0.2 \times 340$ or $0.3 \times 340$ or $0.4 \times 340$<br>or for any <b>full</b> equivalent calculation to these                                                                                                                                                                                                                                |
|          |     | cas                                                                                                                                                                                                                                                  | 102                |      | A1                                                                                                                                                                                                                                                                                                                                                                                 |
|          | (c) | $\frac{0.3}{1 - 0.1} \left[ = \frac{1}{3} \right]$ oe<br>or $\frac{"102"}{340 - 0.1 \times 340} \left[ = \frac{"102"}{306} \right]$ oe                                                                                                               |                    | 3    | M1 Correct probability of red for first counter, given not green. Ft their 102 from part b, if used.                                                                                                                                                                                                                                                                               |
|          |     | $\frac{0.3}{1 - 0.1}$ or $\frac{102}{306} \left[ = \frac{1}{3} \right] \times \frac{"102"-1}{340-1}$ or<br>$\frac{\frac{"102"}{340} \times \frac{"102"-1}{339}}{1 - \frac{"102"/3}{340}} = \left[ \frac{0.3 \times \frac{101}{339}}{0.9} \right]$ oe |                    |      | M1 dep on 1 <sup>st</sup> M<br>Correct method to find probability of red for second counter and multiplication by probability of red for first counter. Ft their 102 from part b, if used.                                                                                                                                                                                         |
|          |     | cas                                                                                                                                                                                                                                                  | $\frac{101}{1017}$ |      | A1 accept awrt 0.099<br>Allow 0.1 from any correct working                                                                                                                                                                                                                                                                                                                         |
|          |     |                                                                                                                                                                                                                                                      |                    |      | <b>Total 7 marks</b>                                                                                                                                                                                                                                                                                                                                                               |

| Question |  | Working                                                         | Answer                                                                                                                                                  | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                                       |
|----------|--|-----------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 23       |  | $3x^2$ or $-15$                                                 |                                                                                                                                                         | 5    | M1 one correct algebraic term correctly differentiated                                                                                                                                                                                                                                                                                                                                      |
|          |  | " $3x^2 - 15 = 0$ " or<br>$[x = ]\sqrt{5}$ or $[x = ]-\sqrt{5}$ |                                                                                                                                                         |      | M1 dep on previous method mark, their derivative = 0<br>dependent also on a derivative in the form<br>$3x^2 + b$ or $ax^2 - 15$ $a, b \neq 0$<br>May be implied by $[x = ]\sqrt{5}$ or $[x = ]-\sqrt{5}$                                                                                                                                                                                    |
|          |  | $(\pm\sqrt{5})^3 - 15 \times (\pm\sqrt{5}) + 5$                 |                                                                                                                                                         |      | M1 dep on previous method mark<br>for substituting <b>any</b> value of $x$ (from previous working)<br>into $x^3 - 15x + 5$<br>Condone use of a decimal here.<br>This mark can be implied by a correct coordinate,<br>decimal or exact.                                                                                                                                                      |
|          |  |                                                                 | $(\sqrt{5}, 5 - 10\sqrt{5})$ oe exact<br>eg $(-\sqrt{5}, 5 - \sqrt{500})$<br>$(-\sqrt{5}, 5 + 10\sqrt{5})$ oe exact<br>eg $(-\sqrt{5}, 5 + \sqrt{500})$ |      | A2 for both coordinates correct<br><br>A1 only<br>for one correct coordinate<br>or<br>all values correct given as decimals awrt 1dp or a mix of<br>surds and decimals<br>$\sqrt{5} = 2.2(36067\dots)$ $5 + 10\sqrt{5} = 27.4$ (27.36067977)<br>$5 + 10\sqrt{5} = -17.4$ (-17.36067977)<br>Allow answers to be given as $x =$ and $y =$ , so long as<br>correctly paired. If seen we can isw |
|          |  | cas - discuss                                                   |                                                                                                                                                         |      | <b>Total 5 marks</b>                                                                                                                                                                                                                                                                                                                                                                        |

| Question |     | Working                                                                                                                                    | Answer | Mark | Notes                                                                                                                                                                                                                                     |
|----------|-----|--------------------------------------------------------------------------------------------------------------------------------------------|--------|------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 24       | (a) | $(18-2r) \times 18 = 12^2$ oe or<br>$(18-r)^2 = 12^2 + r^2$<br>oe eg $\left(18 - \frac{d}{2}\right)^2 = 12^2 + \left(\frac{d}{2}\right)^2$ |        | 3    | M1 correctly form equation using intersecting chord theorem<br>or<br>correct equation using Pythagoras' theorem                                                                                                                           |
|          |     | $36r = 18^2 - 12^2 [=180]$ oe                                                                                                              |        |      | M1 dep on previous M Correctly isolate terms in $r$ and eliminate $r^2$ if using Pythagoras                                                                                                                                               |
|          |     | cas                                                                                                                                        | 5      |      | A1 cao                                                                                                                                                                                                                                    |
| ALT      | (a) | $18 \times PA = 12^2$ oe<br>$(18-d) \times 18 = 12^2$ oe<br>$[PA = 8 \text{ or } d = 10]$                                                  |        |      | M1 Correct equation to find $PA$ or $d$                                                                                                                                                                                                   |
|          |     | $\frac{18-8}{2}$ or $\frac{10}{2}$                                                                                                         |        |      | M1 dep on previous M<br>Correct method to find the radius, using their $PA$                                                                                                                                                               |
|          |     | cas                                                                                                                                        | 5      |      | A1 cao                                                                                                                                                                                                                                    |
|          | (b) | $5 \times \frac{18}{12}$ oe or $(12+x)^2 = 18^2 + x^2$ oe                                                                                  |        | 2    | M1 Correct use of similar triangles, ft their 5 from (a) or correctly forms equation using Pythagoras<br>Allow seen in part (a) if used in part (b)<br>$BQ = CQ$ (equal tangents) so a correct equation also is $(12+CQ)^2 = 18^2 + CQ^2$ |
|          |     | cas                                                                                                                                        | 7.5    |      | A1 oe                                                                                                                                                                                                                                     |

|     |  |                                                                                                                                                                                                                                                                                                                                                             |     |   |                                                                                                                                                                    |
|-----|--|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|---|--------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ALT |  | $[\angle OPC =] \tan^{-1} \frac{5}{12} [= 22.61986....]$ $\tan "22.61986.." = \frac{BQ}{18} \text{ oe}$ <p>or</p> $\left[ \frac{\sin 90}{12} = \frac{\sin(POC)}{13} \right]$ $[POC =] \sin^{-1} \left( \frac{13}{12} \right) = 67.3801.....$ $OPC = 90 - "67.3801....." [= 22.61986....]$ $\frac{\sin "22.61986...."}{BQ} = \frac{\sin "67.3801....."}{18}$ |     | 2 | <p>Full correct method to find angle <math>OPT</math> (= angle <math>BPQ</math>) awrt 23<br/> <b>and</b> correct equation with <math>BQ</math> and this angle.</p> |
|     |  | cas                                                                                                                                                                                                                                                                                                                                                         | 7.5 |   | A1 oe                                                                                                                                                              |
|     |  |                                                                                                                                                                                                                                                                                                                                                             |     |   | <b><i>Total 5 marks</i></b>                                                                                                                                        |

| Question | Working                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | Answer                                         | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                                 |
|----------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 25       | $\left[\overline{OB}=\right]\begin{pmatrix}-8-5\lambda \\ 7+3\lambda\end{pmatrix}\text{ oe eg }\begin{pmatrix}-8 \\ 7\end{pmatrix}+\begin{pmatrix}-5\lambda \\ 3\lambda\end{pmatrix}\text{ eg }\begin{pmatrix}-8 \\ 7\end{pmatrix}+\begin{pmatrix}5\lambda \\ -3\lambda\end{pmatrix}$ $\text{ oe eg }\begin{pmatrix}x+8 \\ y-7\end{pmatrix}=\begin{pmatrix}-5\lambda \\ 3\lambda\end{pmatrix}\text{ eg }\begin{pmatrix}x+8 \\ y-7\end{pmatrix}=\begin{pmatrix}5\lambda \\ -3\lambda\end{pmatrix}$ $\text{ eg }\begin{pmatrix}8 \\ -7\end{pmatrix}+\begin{pmatrix}\sqrt{169-y^2} \\ y\end{pmatrix}=\begin{pmatrix}-5\lambda \\ 3\lambda\end{pmatrix}\text{ or }\begin{pmatrix}5\lambda \\ -3\lambda\end{pmatrix}$ $\text{ eg }\begin{pmatrix}8 \\ -7\end{pmatrix}+\begin{pmatrix}x \\ \sqrt{169-x^2}\end{pmatrix}=\begin{pmatrix}-5\lambda \\ 3\lambda\end{pmatrix}\text{ or }\begin{pmatrix}5\lambda \\ -3\lambda\end{pmatrix}$ |                                                | 5    | <p>M1 Find <math>\overline{OB}</math> by adding <math>\overline{OA}</math> and a multiple of <math>\overline{AB}</math> or place <math>\overline{OB}</math> written with 2 variables equal to a multiple of <math>\overline{AB}</math></p> <p>Condone missing brackets from column vectors.</p>                                                                                       |
|          | $\sqrt{"(-8-5\lambda)"^2+"(7+3\lambda)"^2}=13\text{ oe eg }$ ${"(-8-5\lambda)"^2+"(7+3\lambda)"^2}=13^2$ $\text{ eg if using }5\lambda\text{ and }-3\lambda {"(-8+5\lambda)"^2+"(7-3\lambda)"^2}=169$ $\text{ eg }-7+\sqrt{169-{"(-5\lambda-8)"^2}}=3\lambda\text{ oe including for }5\lambda/-3\lambda$ $\text{ eg }\sqrt{169-{"(3\lambda+7)"^2}}+8=-5\lambda\text{ oe including for }5\lambda/-3\lambda$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                                                |      | <p>M1 Use their <math> \overline{OB} =13</math> to correctly form an equation in their parameter using <math>x^2+y^2=169</math> and their <math>\overline{OB}</math></p>                                                                                                                                                                                                              |
|          | $34\lambda^2+122\lambda-56[=0]\left[\Rightarrow\lambda=\frac{7}{17}\right]\text{ oe }$ $\text{ or if using }5\lambda\text{ and }-3\lambda$ $34\lambda^2-122\lambda-56[=0]\left[\Rightarrow\lambda=-\frac{7}{17}\right]$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                |      | <p>A1 oe Correct three term quadratic gained.</p> <p>Do not need to see <math>=0</math></p> <p>Implied by correct <math>\lambda</math></p>                                                                                                                                                                                                                                            |
|          | $-8-5\times\frac{7}{17}\text{ and }7+3\times\frac{7}{17}\text{ must use }\lambda>-\frac{8}{5}$ $\text{ or if using }5\lambda\text{ and }-3\lambda$ $-8+5\times-\frac{7}{17}\text{ and }7-3\times-\frac{7}{17}\text{ must use }\lambda<\frac{8}{5}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |                                                |      | <p>M1 dep on previous 2 M marks or dep on correct <math>\lambda</math> seen for substituting their <math>\lambda</math> into a correct <math>\overline{OB}</math> to find <b>both</b> coordinates (working must be seen for an incorrect <math>\lambda</math>, allow <math>\lambda</math> to be any other letter throughout)</p> <p>Both correct coordinates can imply this mark.</p> |
|          | cas                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | $\left(-\frac{171}{17}, \frac{140}{17}\right)$ |      | <p>A1</p> <p>oe fractions</p>                                                                                                                                                                                                                                                                                                                                                         |

|      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                                                  |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |
|------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------|---|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ALT1 | $\begin{bmatrix} \overrightarrow{OB} = \overrightarrow{OA} + \overrightarrow{AB} \\ \overrightarrow{OB} = \overrightarrow{OA} + k\overrightarrow{OC} \end{bmatrix}$ $\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -8-5k \\ 7+3k \end{bmatrix} \text{ oe eg } \begin{bmatrix} x+8 \\ y-7 \end{bmatrix} = \begin{bmatrix} -5k \\ 3k \end{bmatrix}$                                                                                                                           |                                                  | 5 | <p>M1 Find <math>\overrightarrow{OB}</math> by adding <math>\overrightarrow{OA}</math> and a multiple of <math>\overrightarrow{AB}</math> or place <math>\overrightarrow{OB}</math> written with 2 variables equal to a multiple of <math>\overrightarrow{AB}</math><br/>Condone missing brackets from column vectors.</p>                                                                                                                                                                                                                                                                                                                                                               |
|      | $\frac{"x+8"}{-5} = k = \frac{"y-7"}{3} \Rightarrow x = \text{ or } y = \textbf{and } x^2 + y^2 = 13^2$ <p>or</p> $\left[ \text{"slope" of } \overrightarrow{OC} = \right] -\frac{3}{5} = \frac{"y-7"}{\textbf{"8+x"}} \left[ \text{"slope" of } \overrightarrow{AB} = \right] \text{ oe}$ <p>eg <math>-3(x+8) = 5(y-7)</math> eg <math>y = -\frac{3}{5}x + \frac{11}{5} \Rightarrow x = \text{ or } y =</math></p> $\left[ x = \frac{-5y+11}{3} \quad y = \frac{3x-11}{-5} \right]$ |                                                  |   | <p>M1 using their <math>\overrightarrow{OB}</math> allow any letters for x and y<br/>Correctly rearrange each component for k and write x in terms of y or y in terms of x<br/>or<br/>correctly use "slope" of <math>\overrightarrow{OC} =</math> "slope" of <math>\overrightarrow{AB}</math> and write x in terms of y or y in terms of x (<b>this approach can imply first M mark</b>)<br/><b>and</b><br/>state <math>x^2 + y^2 = 13^2</math><br/>The rearrangement for k or use of gradient must be correct and checked for their <math>\overrightarrow{OB}</math><br/>the expression for x in terms of y or y in terms of x needs to be present, but doesn't need to be checked.</p> |
|      | $34y^2 - 110y - 1400 [= 0] \text{ or } 34x^2 - 66x - 4104 [= 0] \text{ oe}$ $\left[ \begin{array}{l} \Rightarrow y = \frac{140}{17} = 8.2(35294.....) \\ x = \frac{-171}{17} = -10.0(58823....) \end{array} \right]$                                                                                                                                                                                                                                                                 |                                                  |   | <p>A1 oe Correct three term quadratic gained.<br/>Do not need to see = 0<br/>Look for equivalent coefficients eg<br/><math>17x^2 - 33x - 2052 [= 0]</math> oe<br/><b>Implied by correct x or y allow awrt 1dp</b></p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |
|      | $x = \frac{-5\left(\frac{140}{17}\right) + 11}{3} \text{ or } y = \frac{3\left(-\frac{171}{17}\right) - 11}{-5} \text{ oe}$ <p>or</p> $x = \sqrt{169 - \left(\frac{140}{17}\right)^2} \text{ or } y = \sqrt{169 - \left(-\frac{171}{17}\right)^2}$                                                                                                                                                                                                                                   |                                                  |   | <p>M1 dep on both previous method marks or dep on correct x or y<br/>for substituting their x into a correct expression for y or their y into a correct expression for x<br/>(working must be seen for an incorrect x or y, allow to be any other letters throughout)<br/>Both correct coordinates can imply this mark.</p>                                                                                                                                                                                                                                                                                                                                                              |
|      | cas                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | $\left( -\frac{171}{17}, \frac{140}{17} \right)$ |   | <p>A1<br/>oe fractions</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
|      |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                                                  |   | <b>Total 5 marks</b>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |

|      |                                                                                                                                                                                                                                                                                                                                                            |                                                |   |                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------|---|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| ALT2 | $\begin{bmatrix} \overrightarrow{OB} = \overrightarrow{OA} + \overrightarrow{AB} \\ \overrightarrow{OB} = \overrightarrow{OA} + k\overrightarrow{OC} \end{bmatrix}$ $\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -8-5k \\ 7+3k \end{bmatrix} \text{ oe eg } \begin{bmatrix} x+8 \\ y-7 \end{bmatrix} = \begin{bmatrix} -5k \\ 3k \end{bmatrix}$ |                                                | 5 | <p>M1 Find <math>\overrightarrow{OB}</math> by adding <math>\overrightarrow{OA}</math> and a multiple of <math>\overrightarrow{AB}</math> or place <math>\overrightarrow{OB}</math> written with 2 variables equal to a multiple of <math>\overrightarrow{AB}</math><br/>Condone missing brackets from column vectors.</p>                                                                                                          |
|      | $[8+x=-5k \quad y-7=3k]$ $8+\sqrt{169-y^2}=-5\left(\frac{-7+y}{3}\right) \text{ oe}$ $\text{or } 3\left(\frac{8+x}{-5}\right)=-7+\sqrt{169-x^2} \text{ oe}$                                                                                                                                                                                                |                                                |   | <p>M1 using their <math>\overrightarrow{OB}</math> allow any letters for x and y</p> <p>Correctly rearranges one component for <math>k</math> and correctly substitutes into the other component <b>using</b> <math>x^2 + y^2 = 13^2</math> – this may be implied by a correct quadratic in <math>x</math> or <math>y</math>, usually with a square root sign.</p> <p>Allow any letters for <math>x</math> and <math>y</math></p>   |
|      | $34y^2 - 110y - 1400 [= 0] \text{ or } 34x^2 - 66x - 4104 [= 0] \text{ oe}$ $\left[ \begin{array}{l} \Rightarrow y = \frac{140}{17} = 8.2(35294.....) \\ x = \frac{-171}{17} = -10.0(58823....) \end{array} \right]$                                                                                                                                       |                                                |   | <p>A1 oe Correct three term quadratic gained.<br/>Do not need to see = 0<br/>Look for equivalent coefficients eg <math>17x^2 - 33x - 2052 [= 0]</math> oe<br/><b>Implied by correct x or y allow awrt 1dp</b></p>                                                                                                                                                                                                                   |
|      | $x = \frac{-5\left(\frac{140}{17}\right)+11}{3} \text{ or } y = \frac{3\left(-\frac{171}{17}\right)-11}{-5}$ <p>Or</p> $x = \sqrt{169 - \left(\frac{140}{17}\right)^2} \text{ or } y = \sqrt{169 - \left(-\frac{171}{17}\right)^2}$                                                                                                                        |                                                |   | <p>M1 dep on both previous method marks or dep on correct <math>x</math> or <math>y</math><br/>for substituting their <math>x</math> into a correct expression for <math>y</math> or their <math>y</math> into a correct expression for <math>x</math><br/>(working must be seen for an incorrect <math>x</math> or <math>y</math>, allow to be any other letters throughout)<br/>Both correct coordinates can imply this mark.</p> |
|      | cas                                                                                                                                                                                                                                                                                                                                                        | $\left(-\frac{171}{17}, \frac{140}{17}\right)$ |   | <p>A1<br/>oe fractions</p>                                                                                                                                                                                                                                                                                                                                                                                                          |
|      |                                                                                                                                                                                                                                                                                                                                                            |                                                |   | <b>Total 5 marks</b>                                                                                                                                                                                                                                                                                                                                                                                                                |

| Question | Working                                                                                                                                                                                                                                                                                                                                                                             | Answer | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                                                                           |
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| 26       | $[MC^2] = 24^2 + 64^2 [= 4672]$<br>$[MC] = \sqrt{24^2 + 64^2} [= 8\sqrt{73} = 68.3520....]$                                                                                                                                                                                                                                                                                         |        | 6    | M1 correct full method to find $MC^2$ or $MC$<br>For $MC$ accept awrt 68 – will imply correct method unless from obviously incorrect method.                                                                                                                                                                                                                                                                                    |
|          | $[ME^2] = 32^2 + 9^2 [= 1105]$<br>$[ME] = \sqrt{32^2 + 9^2} [= \sqrt{1105} = 33.24154....]$                                                                                                                                                                                                                                                                                         |        |      | M1 correct full method to find $ME^2$ or $ME$<br>For $ME$ accept awrt 33 – will imply correct method unless from obviously incorrect method.                                                                                                                                                                                                                                                                                    |
|          | $[CE^2] = 24^2 + "33.2"^2$ oe eg $[CE^2] = 24^2 + "1105" [= 1681]$<br>$[CE] = \sqrt{24^2 + "33.2"^2} [CE] = \sqrt{24^2 + "1105" [= 41]}$<br>$[AC^2] = 48^2 + 64^2 [= 6400]$ or $AC = \sqrt{48^2 + 64^2} [= 80]$<br>or $[OC^2] = 24^2 + 32^2 [= 1600]$ or $AC = \sqrt{24^2 + 32^2} [= 40] \Rightarrow$<br>$[AE^2] = "40"^2 + 9^2 [= 1609]$ or $AE = \sqrt{"40"^2 + 9^2} [= 41 = CE]$ |        |      | M1 <b>correct full method</b> to find $CE^2$ or $CE$ or any of the slant edges eg $AE$ .<br>ft their $ME$ – allow anything they believe is their $ME$ , not contradicted by other working.<br>Allow awrt 41 – will imply correct method unless from obviously incorrect method.<br><b>For the first 3 marks, if students don't follow the quickest route, it must be a full method and they may find any equivalent length.</b> |
|          | $"4672" = ("41")^2 + ("33.2")^2 - 2 \times "41" \times "33.2" \cos CEM$                                                                                                                                                                                                                                                                                                             |        |      | M1 for full, correct use of cosine rule to find an <b>equation</b> involving $CEM$ ft their lengths<br>Implied by the next method mark.<br>Follow through their $MC$ , $ME$ and $CE$ if clearly they are using these sides and not contradicted.                                                                                                                                                                                |
|          | $[\cos CEM] = \frac{("41")^2 + ("33.2")^2 - "68.4^2"}{2 \times "41" \times "33.2"} [= -0.6919...]$<br>oe eg $[\cos CEM] = \frac{"1681" + "1105" - "4672"}{2 \times "41" \times "33.2"} [= -0.6919...]$<br>oe eg $[\cos CEM] = \frac{-"1681" - "1105" + "4672"}{-2 \times "41" \times "33.2"} [= -0.6919...]$                                                                        |        |      | M1 Correctly rearranges cosine rule to find an expression for $CEM$<br>ft their lengths, order of operations must be dealt with correctly.<br>Implies the previous method mark<br>Follow through their $MC$ , $ME$ and $CE$ if clearly they are using these sides and not contradicted.                                                                                                                                         |
|          | <b>Remember to look on the diagram for lengths or methods. If there is a contradiction between these, the working space takes precedence.</b><br>cas                                                                                                                                                                                                                                | 134    |      | A1 awrt 134<br>A correct final answer may imply previous method marks (unless from obviously incorrect working).                                                                                                                                                                                                                                                                                                                |
|          |                                                                                                                                                                                                                                                                                                                                                                                     |        |      | <b>Total 6 marks</b>                                                                                                                                                                                                                                                                                                                                                                                                            |

| Question |     | Working                                                                                                                                                             | Answer               | Mark | Notes                                                                                                                                                                                                                                                                                                                                                                                                                                                                |
|----------|-----|---------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------|------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 27       | (a) |                                                                                                                                                                     | $\frac{360}{x+2}$ oe | 1    | B1 oe eg $180 - \frac{180x}{x+2}$                                                                                                                                                                                                                                                                                                                                                                                                                                    |
|          | (b) | $\frac{360}{x} - 9 = \frac{360}{x+2}$<br>oe eg $180 - \frac{180x}{x+2} + 9 = 180 - \frac{180(x-2)}{x}$<br>oe eg $189 - \frac{180x}{x+2} = 180 - \frac{180(x-2)}{x}$ |                      | 3    | M1 Form correct equation but fit their answer for part (a)<br><br>Note from a correct expression in part (a) an equivalent equation is<br>$\left[-\right] \frac{180x}{x+2} + 9 = \left[-\right] \frac{180(x-2)}{x}$                                                                                                                                                                                                                                                  |
|          |     | Eg $360(x+2) - 9x(x+2) = 360x$ oe<br>eg $360x + 720 = 9x^2 + 18x + 360x$<br>$[9x^2 + 18x - 720 = 0]$                                                                |                      |      | M1 for correct method to remove the denominators from the correct equation but<br><b>Condone</b> correct method to remove denominators from<br>$\frac{360}{x} + 9 = \frac{360}{x+2}$<br>$\frac{360}{x} = \frac{360}{x+2} - 9$<br>$\frac{360}{x} = \frac{360}{x+2}$<br>$180 - \frac{180x}{x+2} - 9 = 180 - \frac{180(x-2)}{x}$ oe<br>$\left[-\right] \frac{180x}{x+2} = \left[-\right] \frac{180(x-2)}{x} + 9$<br>$171 - \frac{180x}{x+2} = 180 - \frac{180(x-2)}{x}$ |
|          |     | wr                                                                                                                                                                  | Correctly shown      |      | A1 for fully correct working<br><b>Allow = 0 to be missing on the final answer only</b>                                                                                                                                                                                                                                                                                                                                                                              |

|  |     |                   |   |   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |
|--|-----|-------------------|---|---|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|  | (c) | $(x + 10)(x - 8)$ |   | 2 | <p>M1 correct method to solve quadratic.<br/>If factorising, allow brackets which when expanded give 2 out of 3 terms correct</p> <p>If using formula must use a fully correct formula, but allow one sign error when substituting</p> $\frac{-2 \pm \sqrt{(2)^2 - 4[\times 1] \times (-80)}}{2[\times 1]} \text{ oe}$ <p>If completing the square need to see</p> $(x + 1)^2 + c [= 0] \quad c \neq 0, -80 \text{ oe}$ <p>This mark is for the method shown<br/><math>x = -10</math> or 8 without working scores M0<br/>(as students are told to show clear algebraic working).</p> |
|  |     | wr                | 8 |   | <p>A1 do not accept <math>-10</math> unless rejected<br/>Dep on M1</p>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |
|  |     |                   |   |   | <b><i>Total 6 marks</i></b>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |