

AMC 12 PRACTICE ARCHIVE

2017

12A and 12B papers + answer keys

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Source and use note

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2017 AMC 12A

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Question 1

Not yet answered

Points out of 6

Pablo buys popsicles for his friends. The store sells single popsicles for \$1 each, 3-popsicle boxes for \$2, and 5-popsicle boxes for \$3. What is the greatest number of popsicles that Pablo can buy with \$8?

(A) 8 (B) 11 (C) 12 (D) 13 (E) 15

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 2

Not yet answered

Points out of 6

The sum of two nonzero real numbers is 4 times their product. What is the sum of the reciprocals of the two numbers?

(A) 1 (B) 2 (C) 4 (D) 8 (E) 12

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 3

Not yet answered

Points out of 6

Ms. Carroll promised that anyone who got all the multiple choice questions right on the upcoming exam would receive an A on the exam. Which one of these statements necessarily follows logically?

- (A) If Lewis did not receive an A, then he got all of the multiple choice questions wrong.
- (B) If Lewis did not receive an A, then he got at least one of the multiple choice questions wrong.
- (C) If Lewis got at least one of the multiple choice questions wrong, then he did not receive an A.
- (D) If Lewis received an A, then he got all of the multiple choice questions right.
- (E) If Lewis received an A, then he got at least one of the multiple choice questions right.

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 4

Not yet answered

Points out of 6

Jerry and Silvia wanted to go from the southwest corner of a square field to the northeast corner. Jerry walked due east and then due north to reach the goal, but Silvia headed northeast and reached the goal walking in a straight line. Which of the following is closest to how much shorter Silvia's trip was, compared to Jerry's trip?

(A) 30% (B) 40% (C) 50% (D) 60% (E) 70%

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 5

Not yet answered

Points out of 6

At a gathering of 30 people, there are 20 people who all know each other and 10 people who know no one. People who know each other hug, and people who do not know each other shake hands. How many handshakes occur?

(A) 240 (B) 245 (C) 290 (D) 480 (E) 490

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 6

Not yet answered

Points out of 6

Joy has 30 thin rods, one each of every integer length from 1 cm through 30 cm. She places the rods with lengths 3 cm, 7 cm, and 15 cm on a table. She then wants to choose a fourth rod that she can put with these three to form a quadrilateral with positive area. How many of the remaining rods can she choose as the fourth rod?

(A) 16 (B) 17 (C) 18 (D) 19 (E) 20

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 7

Not yet answered

Points out of 6

Define a function on the positive integers recursively by $f(1) = 2$, $f(n) = f(n - 1) + 2$ if n is even, and $f(n) = f(n - 2) + 2$ if n is odd and greater than 1. What is $f(2017)$?

(A) 2017 (B) 2018 (C) 4034 (D) 4035 (E) 4036

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 8

Not yet answered

Points out of 6

The region consisting of all points in three-dimensional space within 3 units of line segment $\overline{AB}$ has volume 216π . What is the length AB ?

(A) 6 (B) 12 (C) 18 (D) 20 (E) 24

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 9

Not yet answered

Points out of 6

Let S be the set of points (x, y) in the coordinate plane such that two of the three quantities 3 , $x + 2$, and $y - 4$ are equal and the third of the three quantities is no greater than the common value. Which of the following is a correct description of S ?

- (A) a single point
- (B) two intersecting lines
- (C) three lines whose pairwise intersections are three distinct points
- (D) a triangle
- (E) three rays with a common point

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 10

Not yet answered

Points out of 6

Chloé chooses a real number uniformly at random from the interval $[0, 2017]$. Independently, Laurent chooses a real number uniformly at random from the interval $[0, 4034]$. What is the probability that Laurent's number is greater than Chloe's number?

- (A) $\frac{1}{2}$ (B) $\frac{2}{3}$ (C) $\frac{3}{4}$ (D) $\frac{5}{6}$ (E) $\frac{7}{8}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 11

Not yet answered

Points out of 6

Claire adds the degree measures of the interior angles of a convex polygon and arrives at a sum of 2017. She then discovers that she forgot to include one angle. What is the degree measure of the forgotten angle?

- (A) 37 (B) 63 (C) 117 (D) 143 (E) 163

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 12

Not yet answered

Points out of 6

There are 10 horses, named Horse 1, Horse 2, ..., Horse 10. They get their names from how many minutes it takes them to run one lap around a circular race track: Horse k runs one lap in exactly k minutes. At time 0 all the horses are together at the starting point on the track. The horses start running in the same direction, and they keep running around the circular track at their constant speeds. The least time $S > 0$, in minutes, at which all 10 horses will again simultaneously be at the starting point is $S = 2520$. Let $T > 0$ be the least time, in minutes, such that at least 5 of the horses are again at the starting point. What is the sum of the digits of T ?

- (A) 2 (B) 3 (C) 4 (D) 5 (E) 6

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 13

Not yet answered

Points out of 6

Driving at a constant speed, Sharon usually takes 180 minutes to drive from her house to her mother's house. One day Sharon begins the drive at her usual speed, but after driving $\frac{1}{3}$ of the way, she hits a bad snowstorm and reduces her speed by 20 miles per hour. This time the trip takes her a total of 276 minutes. How many miles is the drive from Sharon's house to her mother's house?

(A) 132 (B) 135 (C) 138 (D) 141 (E) 144

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 14

Not yet answered

Points out of 6

Alice refuses to sit next to either Bob or Carla. Derek refuses to sit next to Eric. How many ways are there for the five of them to sit in a row of 5 chairs under these conditions?

(A) 12 (B) 16 (C) 28 (D) 32 (E) 40

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 15

Not yet answered

Points out of 6

Let $f(x) = \sin x + 2 \cos x + 3 \tan x$, using radian measure for the variable x . In what interval does the smallest positive value of x for which $f(x) = 0$ lie?

(A) (0, 1) (B) (1, 2) (C) (2, 3) (D) (3, 4) (E) (4, 5)

Select one:

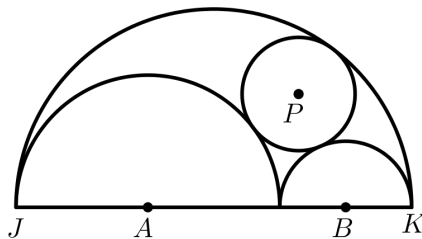
- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 16

Not yet answered

Points out of 6

In the figure below, semicircles with centers at A and B and with radii 2 and 1, respectively, are drawn in the interior of, and sharing bases with, a semicircle with diameter JK . The two smaller semicircles are externally tangent to each other and internally tangent to the largest semicircle. A circle centered at P is drawn externally tangent to the two smaller semicircles and internally tangent to the largest semicircle.



What is the radius of the circle centered at P ?

- (A) $\frac{3}{4}$ (B) $\frac{6}{7}$ (C) $\frac{1}{2}\sqrt{3}$ (D) $\frac{5}{8}\sqrt{2}$ (E) $\frac{11}{12}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 17

Not yet answered

Points out of 6

There are 24 different complex numbers z such that $z^{24} = 1$. For how many of these is z^6 a real number?

- (A) 0 (B) 4 (C) 6 (D) 12 (E) 24

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 18

Not yet answered

Points out of 6

Let $S(n)$ equal the sum of the digits of positive integer n . For example, $S(1507) = 13$. For a particular positive integer n , $S(n) = 1274$. Which of the following could be the value of $S(n + 1)$?

- (A) 1 (B) 3 (C) 12 (D) 1239 (E) 1265

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 19

Not yet answered

Points out of 6

A square with side length x is inscribed in a right triangle with sides of length 3, 4, and 5 so that one vertex of the square coincides with the right-angle vertex of the triangle. A square with side length y is inscribed in another right triangle with sides of length 3, 4, and 5 so that one side of the square lies on the hypotenuse of the triangle. What is $\frac{x}{y}$?

- (A) $\frac{12}{13}$ (B) $\frac{35}{37}$ (C) 1 (D) $\frac{37}{35}$ (E) $\frac{13}{12}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 20

Not yet answered

Points out of 6

How many ordered pairs (a, b) such that a is a positive real number and b is an integer between 2 and 200, inclusive, satisfy the equation $(\log_b a)^{2017} = \log_b(a^{2017})$?

- (A) 198 (B) 199 (C) 398 (D) 399 (E) 597

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 21

Not yet answered

Points out of 6

A set S is constructed as follows. To begin, $S = \{0, 10\}$. Repeatedly, as long as possible, if x is an integer root of some polynomial $a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$ for some $n \geq 1$, all of whose coefficients a_i are elements of S , then x is put into S . When no more elements can be added to S , how many elements does S have?

(A) 4 (B) 5 (C) 7 (D) 9 (E) 11

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 22

Not yet answered

Points out of 6

A square is drawn in the Cartesian coordinate plane with vertices at $(2, 2)$, $(-2, 2)$, $(-2, -2)$, $(2, -2)$. A particle starts at $(0, 0)$. Every second it moves with equal probability to one of the eight lattice points (points with integer coordinates) closest to its current position, independently of its previous moves. In other words, the probability is $1/8$ that the particle will move from (x, y) to each of $(x, y + 1)$, $(x + 1, y + 1)$, $(x + 1, y)$, $(x + 1, y - 1)$, $(x, y - 1)$, $(x - 1, y - 1)$, $(x - 1, y)$, or $(x - 1, y + 1)$. The particle will eventually hit the square for the first time, either at one of the 4 corners of the square or at one of the 12 lattice points in the interior of one of the sides of the square. The probability that it will hit at a corner rather than at an interior point of a side is m/n , where m and n are relatively prime positive integers. What is $m + n$?

(A) 4 (B) 5 (C) 7 (D) 15 (E) 39

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 23

Not yet answered

Points out of 6

For certain real numbers a , b , and c , the polynomial

$$g(x) = x^3 + ax^2 + x + 10$$

has three distinct roots, and each root of $g(x)$ is also a root of the polynomial

$$f(x) = x^4 + x^3 + bx^2 + 100x + c.$$

What is $f(1)$?

(A) -9009 (B) -8008 (C) -7007 (D) -6006 (E) -5005

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 24

Not yet answered

Points out of 6

Quadrilateral $ABCD$ is inscribed in circle O and has side lengths $AB = 3$, $BC = 2$, $CD = 6$, and $DA = 8$. Let X and Y be points on $\overline{BD}$ such that $\frac{DX}{BD} = \frac{1}{4}$ and $\frac{BY}{BD} = \frac{11}{36}$. Let E be the

intersection of line AX and the line through Y parallel to $\overline{AD}$. Let F be the intersection of line CX and the line through E parallel to $\overline{AC}$. Let G be the point on circle O other than C that lies on line CX . What is $XF \cdot XG$?

(A) 17 (B) $\frac{59 - 5\sqrt{2}}{3}$ (C) $\frac{91 - 12\sqrt{3}}{4}$ (D) $\frac{67 - 10\sqrt{2}}{3}$ (E) 18

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 25

Not yet answered

Points out of 6

The vertices V of a centrally symmetric hexagon in the complex plane are given by

$$V = \left\{ \sqrt{2}i, -\sqrt{2}i, \frac{1}{\sqrt{8}}(1+i), \frac{1}{\sqrt{8}}(-1+i), \frac{1}{\sqrt{8}}(1-i), \frac{1}{\sqrt{8}}(-1-i) \right\}.$$

For each j , $1 \leq j \leq 12$, an element z_j is chosen from V at random, independently of the other choices. Let $P = \prod_{j=1}^{12} z_j$ be the product of the 12 numbers selected. What is the probability that $P = -1$?

(A) $\frac{5 \cdot 11}{3^{10}}$ (B) $\frac{5^2 \cdot 11}{2 \cdot 3^{10}}$ (C) $\frac{5 \cdot 11}{3^9}$ (D) $\frac{5 \cdot 7 \cdot 11}{2 \cdot 3^{10}}$ (E) $\frac{2^2 \cdot 5 \cdot 11}{3^{10}}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

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Answer key

1 D	2 C	3 B	4 A	5 B
6 B	7 B	8 D	9 E	10 C
11 D	12 B	13 B	14 C	15 D
16 B	17 D	18 D	19 D	20 E
21 D	22 E	23 C	24 A	25 E



2017 AMC 12B

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Question 1

Not yet answered

Points out of 6

Kymbrea's comic book collection currently has 30 comic books in it, and she is adding to her collection at the rate of 2 comic books per month. LaShawn's collection currently has 10 comic books in it, and he is adding to his collection at the rate of 6 comic books per month. After how many months will LaShawn's collection have twice as many comic books as Kymbrea's?

(A) 1 (B) 4 (C) 5 (D) 20 (E) 25

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 2

Not yet answered

Points out of 6

Real numbers x , y , and z satisfy the inequalities $0 < x < 1$, $-1 < y < 0$, and $1 < z < 2$. Which of the following numbers is necessarily positive?

(A) $y + x^2$ (B) $y + xz$ (C) $y + y^2$ (D) $y + 2y^2$ (E) $y + z$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 3

Not yet answered

Points out of 6

Supposed that x and y are nonzero real numbers such that $\frac{3x + y}{x - 3y} = -2$. What is the value of $\frac{x + 3y}{3x - y}$?

(A) -3 (B) -1 (C) 1 (D) 2 (E) 3

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 4

Not yet answered

Points out of 6

Samia set off on her bicycle to visit her friend, traveling at an average speed of 17 kilometers per hour. When she had gone half the distance to her friend's house, a tire went flat, and she walked the rest of the way at 5 kilometers per hour. In all it took her 44 minutes to reach her friend's house. In kilometers rounded to the nearest tenth, how far did Samia walk?

(A) 2.0 (B) 2.2 (C) 2.8 (D) 3.4 (E) 4.4

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 5

Not yet answered

Points out of 6

The data set $[6, 19, 33, 33, 39, 41, 41, 43, 51, 57]$ has median $Q_2 = 40$, first quartile $Q_1 = 33$, and third quartile $Q_3 = 43$. An outlier in a data set is a value that is more than 1.5 times the interquartile range below the first quartile (Q_1) or more than 1.5 times the interquartile range above the third quartile (Q_3), where the interquartile range is defined as $Q_3 - Q_1$. How many outliers does this data set have?

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 6

Not yet answered

Points out of 6

The circle having $(0, 0)$ and $(8, 6)$ as the endpoints of a diameter intersects the x -axis at a second point. What is the x -coordinate of this point?

- (A) $4\sqrt{2}$ (B) 6 (C) $5\sqrt{2}$ (D) 8 (E) $6\sqrt{2}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 7

Not yet answered

Points out of 6

The functions $\sin(x)$ and $\cos(x)$ are periodic with least period 2π . What is the least period of the function $\cos(\sin(x))$?

- (A) $\frac{\pi}{2}$ (B) π (C) 2π (D) 4π (E) The function is not periodic.

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 8

Not yet answered

Points out of 6

The ratio of the short side of a certain rectangle to the long side is equal to the ratio of the long side to the diagonal. What is the square of the ratio of the short side to the long side of this rectangle?

- (A) $\frac{\sqrt{3}-1}{2}$ (B) $\frac{1}{2}$ (C) $\frac{\sqrt{5}-1}{2}$ (D) $\frac{\sqrt{2}}{2}$ (E) $\frac{\sqrt{6}-1}{2}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 9

Not yet answered

Points out of 6

A circle has center $(-10, -4)$ and has radius 13. Another circle has center $(3, 9)$ and radius $\sqrt{65}$. The line passing through the two points of intersection of the two circles has equation $x + y = c$. What is c ?

- (A) 3 (B) $3\sqrt{3}$ (C) $4\sqrt{2}$ (D) 6 (E) $\frac{13}{2}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 10

Not yet answered

Points out of 6

At Typico High School, 60% of the students like dancing, and the rest dislike it. Of those who like dancing, 80% say that they like it, and the rest say that they dislike it. Of those who dislike dancing, 90% say that they dislike it, and the rest say that they like it. What fraction of students who say they dislike dancing actually like it?

- (A) 10% (B) 12% (C) 20% (D) 25% (E) $\frac{100}{3}\%$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 11

Not yet answered

Points out of 6

Call a positive integer *monotonous* if it is a one-digit number or its digits, when read from left to right, form either a strictly increasing or a strictly decreasing sequence. For example, 3, 23578, and 987620 are *monotonous*, but 88, 7434, and 23557 are not. How many *monotonous* positive integers are there?

- (A) 1024 (B) 1524 (C) 1533 (D) 1536 (E) 2048

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 12

Not yet answered

Points out of 6

What is the sum of the roots of $z^{12} = 64$ that have a positive real part?

- (A) 2 (B) 4 (C) $\sqrt{2} + 2\sqrt{3}$ (D) $2\sqrt{2} + \sqrt{6}$ (E) $(1 + \sqrt{3}) + (1 + \sqrt{3})i$

Select one:

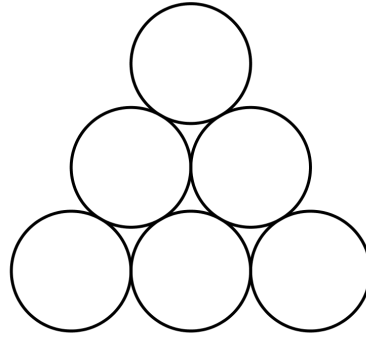
- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 13

Not yet answered

Points out of 6

In the figure below, 3 of the 6 disks are to be painted blue, 2 are to be painted red, and 1 is to be painted green. Two paintings that can be obtained from one another by a rotation or a reflection of the entire figure are considered the same.



How many different paintings are possible?

- (A) 6 (B) 8 (C) 9 (D) 12 (E) 15

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 14

Not yet answered

Points out of 6

An ice-cream novelty item consists of a cup in the shape of a 4-inch-tall frustum of a right circular cone, with a 2-inch-diameter base at the bottom and a 4-inch-diameter base at the top, packed solid with ice cream, together with a solid cone of ice cream of height 4 inches, whose base, at the bottom, is the top base of the frustum. What is the total volume of the ice cream, in cubic inches?

- (A) 8π (B) $\frac{28\pi}{3}$ (C) 12π (D) 14π (E) $\frac{44\pi}{3}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 15

Not yet answered

Points out of 6

Let ABC be an equilateral triangle. Extend side $\overline{AB}$ beyond B to a point B' so that $BB' = 3AB$. Similarly, extend side $\overline{BC}$ beyond C to a point C' so that $CC' = 3BC$, and extend side $\overline{CA}$ beyond A to a point A' so that $AA' = 3CA$. What is the ratio of the area of $\triangle A'B'C'$ to the area of $\triangle ABC$?

- (A) 9 : 1 (B) 16 : 1 (C) 25 : 1 (D) 36 : 1 (E) 37 : 1

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 16

Not yet answered

Points out of 6

The number $21! = 51,090,942,171,709,440,000$ has over 60,000 positive integer divisors. One of them is chosen at random. What is the probability that it is odd?

- (A) $\frac{1}{21}$ (B) $\frac{1}{19}$ (C) $\frac{1}{18}$ (D) $\frac{1}{2}$ (E) $\frac{11}{21}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 17

Not yet answered

Points out of 6

A coin is biased in such a way that on each toss the probability of heads is $\frac{2}{3}$ and the probability of tails is $\frac{1}{3}$. The outcomes of the tosses are independent. A player has the choice of playing Game A or Game B. In Game A she tosses the coin three times and wins if all three outcomes are the same. In Game B she tosses the coin four times and wins if both the outcomes of the first and second tosses are the same and the outcomes of the third and fourth tosses are the same. How do the chances of winning Game A compare to the chances of winning Game B?

- (A) The probability of winning Game A is $\frac{4}{81}$ less than the probability of winning Game B.
- (B) The probability of winning Game A is $\frac{2}{81}$ less than the probability of winning Game B.
- (C) The probabilities are the same.
- (D) The probability of winning Game A is $\frac{2}{81}$ greater than the probability of winning Game B.
- (E) The probability of winning Game A is $\frac{4}{81}$ greater than the probability of winning Game B.

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 18

Not yet answered

Points out of 6

The diameter AB of a circle of radius 2 is extended to a point D outside the circle so that $BD = 3$. Point E is chosen so that $ED = 5$ and line ED is perpendicular to line AD . Segment AE intersects the circle at a point C between A and E . What is the area of $\triangle ABC$?

- (A) $\frac{120}{37}$ (B) $\frac{140}{39}$ (C) $\frac{145}{39}$ (D) $\frac{140}{37}$ (E) $\frac{120}{31}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 19

Not yet answered

Points out of 6

Let $N = 123456789101112 \dots 4344$ be the 79-digit number that is formed by writing the integers from 1 to 44 in order, one after the other. What is the remainder when N is divided by 45?

- (A) 1 (B) 4 (C) 9 (D) 18 (E) 44

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 20

Not yet answered

Points out of 6

Real numbers x and y are chosen independently and uniformly at random from the interval $(0, 1)$. What is the probability that $\lfloor \log_2 x \rfloor = \lfloor \log_2 y \rfloor$, where $\lfloor r \rfloor$ denotes the greatest integer less than or equal to the real number r ?

- (A) $\frac{1}{8}$ (B) $\frac{1}{6}$ (C) $\frac{1}{4}$ (D) $\frac{1}{3}$ (E) $\frac{1}{2}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 21

Not yet answered

Points out of 6

Last year, Isabella took 7 math tests and received 7 different scores, each an integer between 91 and 100, inclusive. After each test she noticed that the average of her test scores was an integer. Her score on the seventh test was 95. What was her score on the sixth test?

- (A) 92 (B) 94 (C) 96 (D) 98 (E) 100

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 22

Not yet answered

Points out of 6

Abby, Bernardo, Carl, and Debra play a game in which each of them starts with four coins. The game consists of four rounds. In each round, four balls are placed in an urn---one green, one red, and two white. The players each draw a ball at random without replacement. Whoever gets the green ball gives one coin to whoever gets the red ball. What is the probability that, at the end of the fourth round, each of the players has four coins?

- (A) $\frac{7}{576}$ (B) $\frac{5}{192}$ (C) $\frac{1}{36}$ (D) $\frac{5}{144}$ (E) $\frac{7}{48}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 23

Not yet answered

Points out of 6

The graph of $y = f(x)$, where $f(x)$ is a polynomial of degree 3, contains points $A(2, 4)$, $B(3, 9)$, and $C(4, 16)$. Lines AB , AC , and BC intersect the graph again at points D , E , and F , respectively, and the sum of the x -coordinates of D , E , and F is 24. What is $f(0)$?

- (A) -2 (B) 0 (C) 2 (D) $\frac{24}{5}$ (E) 8

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 24

Not yet answered

Points out of 6

Quadrilateral $ABCD$ has right angles at B and C , $\triangle ABC \sim \triangle BCD$, and $AB > BC$. There is a point E in the interior of $ABCD$ such that $\triangle ABC \sim \triangle CEB$ and the area of $\triangle AED$ is 17 times the area of $\triangle CEB$. What is $\frac{AB}{BC}$?

- (A) $1 + \sqrt{2}$ (B) $2 + \sqrt{2}$ (C) $\sqrt{17}$ (D) $2 + \sqrt{5}$ (E) $1 + 2\sqrt{3}$

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

Question 25

Not yet answered

Points out of 6

A set of n people participate in an online video basketball tournament. Each person may be a member of any number of 5-player teams, but no two teams may have exactly the same 5 members. The site statistics show a curious fact: The average, over all subsets of size 9 of the set of n participants, of the number of complete teams whose members are among those 9 people is equal to the reciprocal of the average, over all subsets of size 8 of the set of n participants, of the number of complete teams whose members are among those 8 people. How many values n , $9 \leq n \leq 2017$, can be the number of participants?

- (A) 477 (B) 482 (C) 487 (D) 557 (E) 562

Select one:

- ☐ A
- ☐ B
- ☐ C
- ☐ D
- ☐ E
- ☐ Leave blank (1.5 points)

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Answer key

1 E	2 E	3 D	4 C	5 B
6 D	7 B	8 C	9 A	10 D
11 B	12 D	13 D	14 E	15 E
16 B	17 D	18 D	19 C	20 D
21 E	22 B	23 D	24 D	25 D